# Anekant Education Society's Tuljaram Chaturchand College of Arts, Science and Commerce, Baramati

# Autonomous

**Course Structure for B.Sc. Mathematics (w.e.f. 2022-23)** 

Semester	Course	Title of Course	No. of Credits	No. of
	Code		Creuits	Lectures
	USMT111	Algebra	2	36
Ι	USMT112	Calculus-I	2	36
	USMT113	Practical based on USMT111 and USMT112	2	48
	USMT121	Geometry	2	36
II	USMT122	Calculus and Differential Equations	2	36
	USMT123	Practical based on USMT121 and USMT122	2	48

## F. Y. B. Sc. Mathematics

#### S. Y. B. Sc. Mathematics

Semester	Course	Title of Course	No. of	No. of
	Code		Credits	Lectures
	USMT231	Calculus of Several Variables	3	48
III	USMT232	Laplace Transform & Fourier Series	3	48
	USMT233	Practical based on USMT231 and USMT232	2	48
	USMT241	Vector Calculus	3	48
IV	USMT242	Linear Algebra	3	48
	USMT243	Practical based on USMT241 and USMT242	2	48

### T.Y.B.Sc Mathematics

Semester	Course Code	Title of Course	No. of	No. of
			Credits	Lectures
	USMT351	Metric Spaces	3	48
	USMT352	Real Analysis I	3	48
	USMT353	Group Theory	3	48
	USMT354	Ordinary Differential Equation	3	48
	USMT355	Number Theory	3	48
	USMT356(A)	Operation Research	3	48
	USMT356(B)	C Programming	3	48
	USMT357	Practical based on USMT351 and USMT352	2	48
	USMT358	Practical based on USMT353 and USMT354	2	48
	USMT359	Practical based on USMT355 and USMT356	2	48
VI	USMT361	Complex Analysis	3	48
V I	USMT362	Real Analysis II	3	48
	USMT363	Ring Theory	3	48
	USMT364	Partial Differential Equation	3	48

USMT365	Lebesgue Integration	3	48
USMT366(A)	Optimization Techniques	3	48
USMT366(B)	Python Programming	3	48
USMT367	Practical based on USMT361, USMT362, and USMT363	2	48
USMT368	Practical based on USMT364, USMT365, and USMT366	2	48
USMT369	Mathematics Project	2	48

# Equivalence of the old syllabus with the new syllabus

Old Course		New Course		
MAT 1201	Geometry	USMT121	Geometry	
MAT 1202	Calculus-II	USMT122	Calculus and Differential Equations	
MAT 1203	Practical based on MAT 1101 and MAT 1102	USMT123	Practical based on USMT121 and USMT122	

#### Academic Year 2022-23

Class: F.Y.B.Sc. (Semester – II)

Paper Code: USMT121

Paper: I

Credit: 2

Title of the Paper: Geometry No. of Lectures: 36

#### A) Learning Objectives:

- To introduce analytical geometry of 2 and 3 dimensions.
- To study characteristics of 2 and 3 dimensional geometric shapes and mathematical results about their relationships.
- To develop a positive attitude towards Mathematics as an interesting and valuable subject of study.

#### **B)** Learning Outcomes:

- Students will be able to perform translations and rotations in 2 dimensions.
- Students will be able to identify lines, planes and spheres in 3 dimensions from equation.
- Students will be able to apply appropriate formulas and tools to determine measurements and use these techniques in real life context and other disciplines.

#### **TOPICS/CONTENTS:**

#### **Unit 1: Analytical Geometry of two dimensions** [10 Lectures]

- 1.1 Change of axes: Translation and Rotation
- 1.2 General equation of second degree in two variables
- 1.3 Reduction to standard form

#### Unit 2: Planes in three dimensions

- 2.1 Direction cosines and direction ratios
- 2.2 Equation of the plane: Normal form, Transform to the normal form
- 2.3 Planes passing through three non-collinear points
- 2.4 Intercept form
- 2.5 Angle between two planes
- 2.6 Distance of a point from a plane
- 2.7 Distance between parallel planes
- 2.8 System of planes
- 2.9 Two sides of planes
- 2.10 Bisectors of angles between two planes

[10 Lectures]

#### **Unit 3: Lines in three dimensions**

[8 Lectures]

- 3.1 Equations of lines in symmetric and asymmetric forms
- 3.2 Line passing through two points
- 3.3 Angle between a line and a plane
- 3.4 Coplanar lines
- 3.5 Skew lines
- 3.6 Distance of a point from a line

#### **Unit 4: The Sphere**

- 4.1 Equation of a sphere
- 4.2 Plane section of a sphere
- 4.3 Intersection of two spheres
- 4.4 Sphere through a given circle
- 4.5 Intersection of a sphere and a line
- 4.6 Equation of tangent plane

#### **Text Books:**

- 1. Analytic Geometry in Two and Three Dimensions, *Von Steuben* Unit 1: Sections: 8.4.
- Analytical Solid Geometry, *Shantinarayan*, S. Chand and Company Ltd., New Delhi, 1998.
  Unit 2: Sections: 1.6, 1.7, 2.1 to 2.7; Unit 3: Sections: 3.1 to 3.4, 3.7;

**Unit 4:** Sections: 6.1 to 6.6.

#### **Reference Books:**

- 1. Analytical Geometry of 2D and 3D, P. R. Vittal, Pearson, 2013.
- 2. A Textbook of Two Dimensional Geometry, *Sat Pal* and *Harbans Lal*, New Age International Publishers.
- 3. Textbook of Analytical Geometry of Three Dimensions, *P. K. Jain* and *Khalil Ahmad*, New Age International Publishers.
- 4. Theory and Problems of Plane and Solid Analytic Geometry, *Joseph H. Kindle*, Schaum's Outline Series.

#### [8 Lectures]

Class: F.Y. B. Sc. (Semester- II) Paper Code: USMT122 Paper: II **Title of Paper:** Calculus and Differential Equations **Credit:** 2 **No. of lectures:** 36

#### A) Learning Objectives:

- To understand the idea of differentiation from first principles.
- To understand and work with derivatives as rates of change in mathematical models.
- To understand the use of both graphical and numerical methods.

#### **B)** Learning Outcome:

- Students will recognize problem solving techniques appropriate to a given situation including the development of mathematical models.
- Students will able to determine the rate of change of a quantity with respect to another quantity.

#### Unit 1: Differentiation

#### [12 lectures]

**1.1** The Derivative:

The definition of derivative at a point, relationship between differentiability and continuity, Rules for Differentiation, Caratheodory's Theorem (without Proof), The Chain Rule, Derivative of inverse function.

**1.2** The Mean Value Theorem:

Interior Extremum Theorem, Rolle's Theorem, Mean Value Theorem, Cauchy Mean Value Theorem, Intervals of increasing and decreasing functions, First Derivative Test for Maxima, Intermediate Value Theorem, Darboux's Theorem.

#### Unit 2:L'Hospital's Rule and Successive Differentiation [14 lectures]

**2.1** L'Hospital Rule: Indeterminate Forms, L'Hospital Rules (without proof)

**2.2** Taylor's Theorem: Taylor's Theorem (without proof), MacLaurin's theorem with Lagrange's form remainder

**2.3** Successive Differentiation: The n<sup>th</sup> derivative and Leibnitz theorem for successive differentiation.

#### Unit 3: Ordinary Differential Equations [10 lectures]

**3.1** First Order Differential Equations: First order linear differential equation, separable equations, Homogeneous equations

**3.2** Orthogonal Trajectories: Formation of Differential equation, orthogonal trajectory, Existence and uniqueness of solutions

**3.3** Exact Equations: Exact differential equations, Integrating Factors.

#### **Textbooks:**

- 1. Introduction to Real Analysis by R.G. Bartle and D.R. Sherbert, John Wiley and Sons Inc, Fourth Edition.
  - Unit 1: Sec 6.1 and Sec. 6.2, Unit 2: Sec 6.3 and Sec. 6.4
- Differential Equations by George F. Simmons, Steven G. Krantz, Tata McGrawHill. Unit 3: Sec 1.3 to Sec 1.8

#### **Reference books:**

**1.** Introduction to Real analysis, William F.Trench, Free edition, 2010.

2. Calculus of a single variable Ron Larson, Bruce Edwards, tenth edition.

**3**. Elementary Analysis, The Theory of Calculus, Kenneth A. Ross, Springer Publication, second edition.

**4**. Calculus and its Applications, Marvin L. Bittinger, David J. Ellenbogen and Scott A. Surgent, Addison Wesley, tenth edition.

**5**. Ordinary and Partial Differential Equation, by M.D.Raisinghania, S.Chand and Company LTD, 2009.

6. Daniel Murray, Introductory Course in Differential Equations, Orient Longman

Class: F.Y. B. Sc. (Semester- II)Title of Paper: Practical Based on USMT121 & USMT122Paper Code: USMT123Credit: 2Paper: IIINo. of lectures: 48

#### A) Learning Objectives:

- Improve problem-solving ability in Geometry of two and three dimensions
- Improve problem-solving ability in Differentiation and Differential equations
- Use of ICT tools to learn Mathematics.

#### **B) Learning Outcome:**

- Lead students to learn and improve their understanding of Mathematics.
- Students will be able to analyze geometrical properties of two- and three-dimensional shapes and develop mathematical arguments about geometric relationships. Also, they will be to solve and apply derivatives of different functions.

#### **Title of Experiments:**

- 1. Analytical Geometry of two dimensions
- 2. Planes in three dimensions
- 3. Lines in three dimensions
- 4. Sphere
- 5. History of Geometry
- 6. Geometry using Maxima Software
- 7. Differentiation
- 8. Mean Value Theorem
- 9. L'Hospital's Rule
- 10. Successive Differentiation
- 11. Ordinary Differential Equations
- 12. Differentiability using Maxima Software